

[2] involuteΣ Bevel Gear Design System

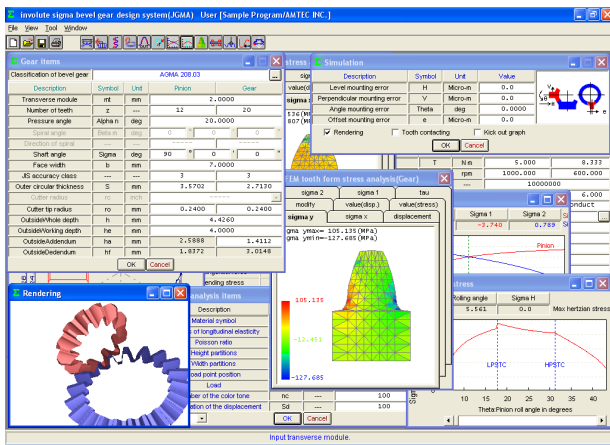


Fig. 2.1 involuteΣ Bevel Gear Design System

2.1 Introduction

The *involuteΣ Bevel Gear Design System* is a complete design system for bevel gears. It offers Gear Dimension, Strength Calculation (Metal or Resin), Tooth Profile Rendering, Assembly Drawing, Bearing Load Calculation, Sliding Ratio Graph, Hertzian Stress Graph, Profile Tooth Stress Analysis, Tooth Contact Area Display, Measurement Data Output, and many other features.

2.2. Software Features

Table 2.1 shows the available software features offered.

Table 2.1. Software Features

Item	Page	Straight	Spiral
<1> Gear Dimension	8	<input type="radio"/>	<input type="radio"/>
<2> Gear Meshing Drawing	8	<input type="radio"/>	<input type="radio"/>
<3> Gear Assembly Drawing	8	<input type="radio"/>	<input type="radio"/>
<4> Tooth Profile DXF File Output	8	<input type="radio"/>	<input type="radio"/>
<5> Strength Calculation (Metal)	9	<input type="radio"/>	<input type="radio"/>
<6> Strength Calculation (Resin)	---	<input type="radio"/>	<input type="radio"/>
<7> Gear Accuracy	9	<input type="radio"/>	<input type="radio"/>
<8> Design Data Control	---	<input type="radio"/>	<input type="radio"/>
<9> Tooth Profile Rendering	10	<input type="radio"/>	<input type="radio"/>
<10> Sliding Ratio Graph	11	<input checked="" type="radio"/>	<input type="radio"/>
<11> Hertzian Stress Graph	11	<input checked="" type="radio"/>	<input type="radio"/>
<12> Crossed Axes Angle (Acute)	11	<input checked="" type="radio"/>	<input type="radio"/>
<13> 3D Tooth Profile Coordinate Output	10	<input checked="" type="radio"/>	<input type="radio"/>
<14> Tooth Profile IGES File Output ¹⁾	11	<input checked="" type="radio"/>	<input type="radio"/>
<15> Tooth Profile IGES File Output for FEM Analysis ¹⁾	11	<input checked="" type="radio"/>	<input type="radio"/>
<16> Assembly Error Simulation	11	<input checked="" type="radio"/>	<input type="radio"/>
<17> Over-Ball Diameter Measurement ¹⁾	10	<input checked="" type="radio"/>	<input checked="" type="radio"/>
<18> 2D-FEM Tooth Profile Stress Analysis ¹⁾	10	<input checked="" type="radio"/>	<input checked="" type="radio"/>
<19> Tooth Profile Measurement ¹⁾	11	<input checked="" type="radio"/>	<input type="radio"/>
<20> Tooth Contact Area ¹⁾	11	<input checked="" type="radio"/>	<input type="radio"/>
<21> STL File Output ¹⁾	11	<input checked="" type="radio"/>	<input type="radio"/>
<22> Crossed Axes Angle (Acute)	---	<input checked="" type="radio"/>	<input type="radio"/>
<23> Chamfer Shape	9	<input checked="" type="radio"/>	<input type="radio"/>
<24> Kick Out Graph	10	<input checked="" type="radio"/>	<input type="radio"/>
<25> Minimum of 9 Teeth	---	<input checked="" type="radio"/>	<input type="radio"/>

(Supported as standard) (Optional)

1) "<13> 3D Tooth Profile Coordinate" software is required.

2.3 Icon Buttons

The toolbar contains 13 icon buttons including [Dimension], [Assembly], [Profile], and [Rendering].



2.4 Supported Gear Types

The System supports 14 types of bevel gears: six spur bevel gears and eight spiral bevel gears. Fig. 2.2 shows the supported bevel gear types.



Fig. 2.2 Supported Bevel Gear Types

2.5 Gear Dimensions

Selecting a bevel gear type in Fig. 2.2 displays the Gear dimension input screen as shown in Fig. 2.3. After specifying the module and number of teeth of the pinion/gear, pressing the TAB key sets the default values for the remaining items (editable). The System not only supports shaft angles of other than 90 degrees, but also calculates the inclined and constant height teeth.

The Modified gear dimension input screen shown in Fig. 2.4 allows the user to specify the tip modification and crowning data and change the tip and root angles of the bevel gear as desired.

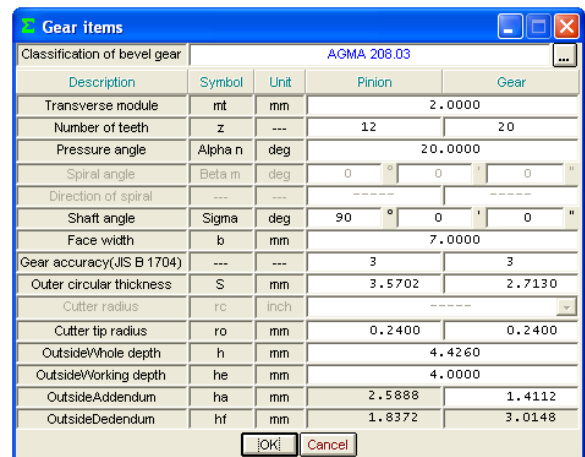


Fig. 2.3 Gear Dimension Input Screen

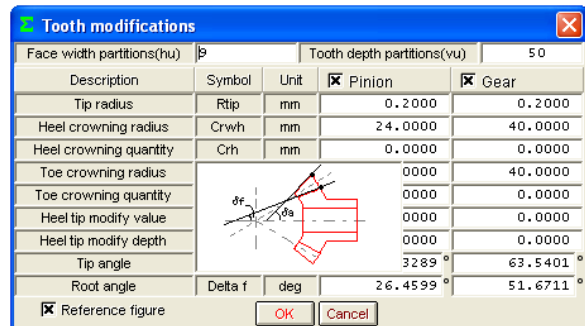


Fig. 2.4 Modified Gear Dimension Input Screen

2.6 Gear Dimensions Calculation

The calculated dimensions of the bevel gear are displayed in the Gear dimension calculation result screen shown in Fig. 2.5.

Description	Symbol	Unit	Pinion	Gear
Outer cone distance	Re	mm	23.3238	
Pitch diameter	d	mm	24.0000	40.0000
Outside diameter	dae	mm	28.4398	41.4521
Inside diameter	dai	mm	19.6851	28.8798
Pitch cone angle	Delta	deg	30° 57' 50"	59° 2' 10"
Addendum	ha	mm	2.5888	1.4112
Dedendum	hf	mm	1.8372	3.0148
Clearance	c	mm	0.4260	0.4260
Addendum angle	Theta a	deg	7° 21' 55"	4° 30' 14"
Dedendum angle	Theta f	deg	4° 30' 14"	7° 21' 55"
Tip cone angle	Delta a	deg	38° 19' 44"	63° 32' 24"
Root cone angle	Delta f	deg	26° 27' 36"	51° 40' 16"
Working depth	he	mm	4.0000	
Whole depth	h	mm	4.4260	
Distance of outside tip from conic top	X	mm	18.6681	10.7899
Axial face width	Xb	mm	5.5369	3.1287
Circular thinning for backlash	fn	mm	0.0000	
Backlash	BL	mm	0.0000	
Tooth angle	---	min	361.6955	361.6972
Material angle	Theta x	deg	82° 38' 6"	85° 29' 46"
Material angle	Theta y	deg	59° 2' 10"	30° 57' 50"
Chordal thickness	Sj	mm	3.5570	2.7109
Chordal addendum	Hj	mm	2.7027	1.4349
Equivalent number of teeth	Zv	---	13.9943	38.8730
Transverse contact ratio	Epsiro alpha	---	1.3896	
Overlap ratio	Epsiro beta	---	0.0000	
Total contact ratio	Epsiro gamma	---	1.3896	

Fig. 2.5 Calculated Gear Dimensions

2.7 Gear Assembly Drawing

As shown in Fig. 2.6, assembly drawings can be produced by specifying the length and boss diameter information on the pinion and gear pair. Fig. 2.6a is an example of chamfering the outer diameter and boss ends of the pinion for the forging process. In addition, Fig. 2.7 and Fig. 2.8 are drawing examples for setting the shaft angle to 70 degrees and 120 degrees, respectively. Assembly drawings can be output in the DXF file format.

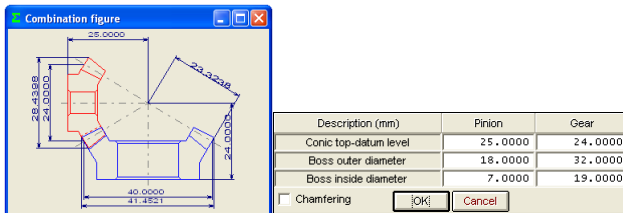


Fig. 2.6 Gear Assembly Drawing and Settings

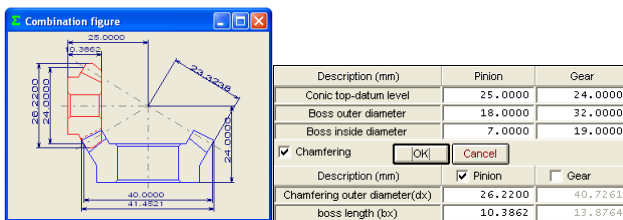


Fig. 2.6a Gear Assembly Drawing and Settings (Chamfering)

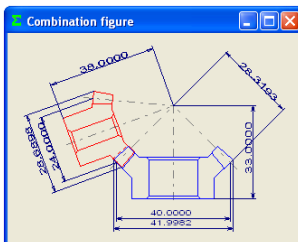


Fig. 2.7 Assembly Drawing
(Shaft Angle = 70°)

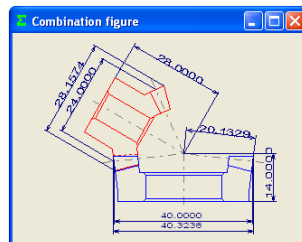


Fig. 2.8 Assembly Drawing
(Shaft Angle = 120°)

2.8 Gear Profile Drawing

Gear profile drawings showing how the gear is meshed with the pinion at the outer end, center, or inner end can be drawn. Fig. 2.9 is a gear profile meshing drawing for the outer end.

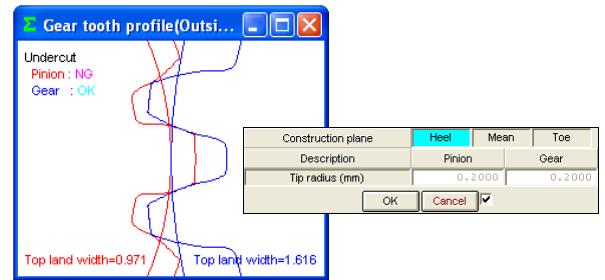


Fig. 2.9 Gear Meshing Drawing

2.9 Assembly Error Simulation

Improperly assembled gear pair would cause the variation of the point of contact when the pinion and gear are in mesh. By setting the Assembly Error Simulation, the user can observe this variation using the Tooth Profile Rendering and Tooth Contact Variation features to evaluate the impact of horizontal, vertical, angular, and offset errors in the gear assembly.

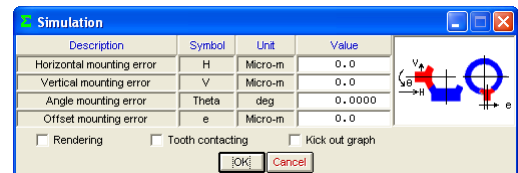


Fig. 2.10 Assembly Error Simulation Settings

2.10 Tooth Profile Rendering

3D tooth profiles of the pinion and gear in mesh can be generated as shown in Fig. 2.11. The generated tooth profiles will be based on spherical involutes and theoretical leads. The viewing angle of the image can be changed using the control form shown in Fig. 2.11. Setting the meshing step angle to "1" causes the pinion to rotate in increments of 1 degree; entering "0" produces a still image. The generated profile images are scalable.

Fig. 2.12 and Fig. 2.13 show the 3D rendering images that represent the tooth profiles of spiral bevel and Zerol gears, respectively.

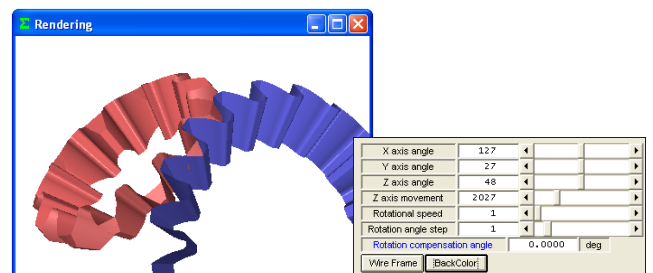


Fig. 2.11 Tooth Profile Rendering Image and Settings

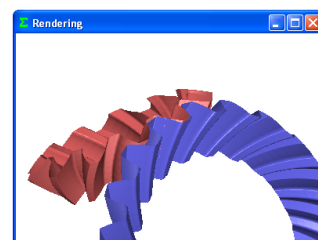


Fig. 2.12 Spiral Bevel Gears

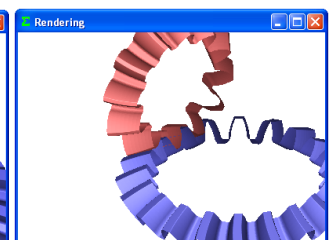


Fig. 2.13 Zerol Gears

2.11 Tooth Contact Variation

Fig. 2.14 shows the point of contact on the pinion tooth flank when crowning is specified on the Modified gear dimension input screen in Fig. 2.4. The pinion will be completely in contact with the gear at the flank area shown in red but, in blue area, there is a clearance of 50- μ m from the tooth flank of the mating gear. The user can change the pinion rotation angle in the control form to see how the contact area moves. Fig. 2.14a and Fig. 2.14b show contact area of spiral bevel and zerol pinions, respectively.

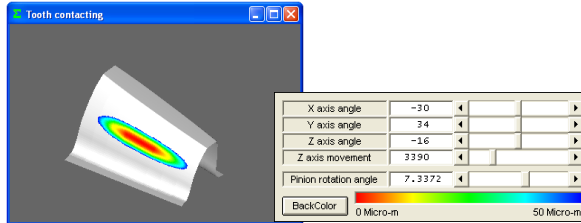


Fig. 2.14 Tooth Contact Area (Straight Bevel)

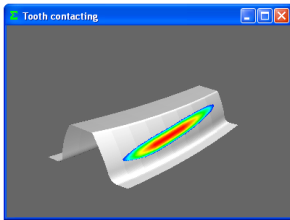


Fig. 2.14a Tooth Contact Area (Spiral)

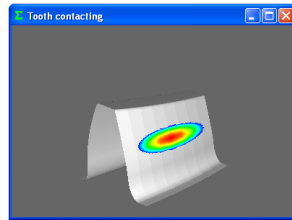


Fig. 2.14b Tooth Contact Area (Zerol)

2.12 Kick Out Graph

The Kick Out feature simulates the circumferential play ("kick out") in the gear from the start to the end of meshing with the pinion. As shown in Fig. 2.15, the kick out value is only "0.0007" degree when the gearshaft mounting error is 0. However, changing both the horizontal and vertical errors in gear shaft mounting to 5 μ m in Fig. 2.10 will increase the kick out value to "0.0093" degree as shown in Fig. 2.16, significantly changing the kick-out curve.

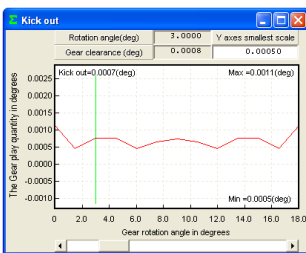


Fig. 2.15 Kick Out Graph 1

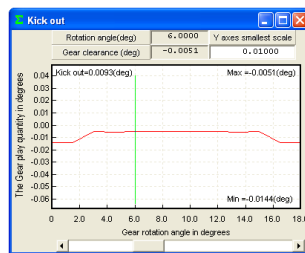


Fig. 2.16 Kick Out Graph 2

2.13 Tooth Profile Data Output

As shown in Fig. 2.17, the user can choose to output the assembly drawing, 3D tooth profile, or 3D meshing tooth profile image into a data file. Fig. 2.18 is an example of a 3D pinion tooth profile output file displayed in a CAD system. Fig. 2.19 is an example of 3D meshing tooth profile image output for FEM analysis, where the tooth profile data will be output into separate files for the left/right flank and tip portions.



Fig. 2.17 Tooth Profile Data File Output

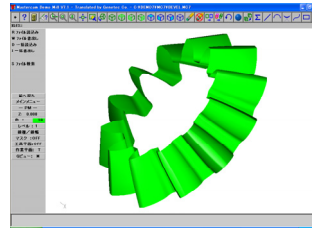


Fig. 2.18 3D Pinion Tooth Profile (IGES)

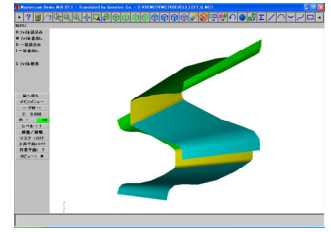


Fig. 2.19 3D Meshing Tooth Profile (IGES)

2.14 Gear Strength Calculation

(1) Torque Unit Setting (N·m, N·cm, kgf·m, kgf·cm, gf·cm)

Fig. 2.20 shows the Torque unit tab of the Initial strength calculation settings screen.



Fig. 2.20 Initial Strength Calculation Settings Screen (Torque Unit Tab)

(2) Bevel Gear Strength Calculation

The System calculates the strength of metal gears based on the JGMA 403-01 and 404-01 standards. For resin gears, the calculation of the bending strength is based on the Lewis formula and the strength of the tooth flank on the Hertzian stress.

(3) Materials

Fig. 2.21 shows the Metal material tab of the Initial Strength Calculation Settings screen. The stress values shown in the Resin material tab are experimental values taking into account the temperature and life cycle of the resin material.

The applicable materials are M90, KT20, and GH25. The characteristics of other material can be calculated based on M90.

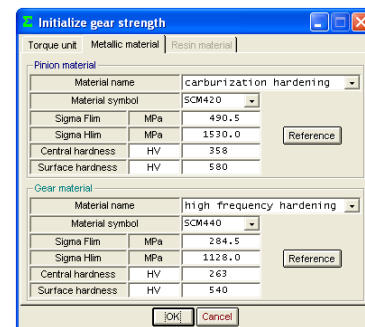


Fig. 2.21 Initial Strength Calculation Settings Screen (Metal material Tab)

(4) Material Selection

Clicking the [Reference] button in Fig. 2.21 displays the material selection screen as shown in Fig. 2.22. On this screen, the user can determine the allowable stress value for the material based on the hardness values shown in the list. The material symbol and the allowable stress ($\hat{\sigma}_{Flim}$, $\hat{\sigma}_{Hlim}$) and hardness values can be specified directly on the Metal material tab.

Structural alloy steel	Mechanical properties			Effective carburizing	Hardness		
	HB	HV	MPa		HV	HRC	MPa
SCM415	220	281	333.5	Comparatively light	580	5.4	1284.5
	230	242	353		600	5.5	1314
	240	252	372.5		620	5.6	1343.5
	250	262	392.5		640	5.7	1373.5
	260	273	402		660	5.8	1383.5
SCM420	270	284	417	Comparatively light	680	5.9	1353.5
	280	295	431.5		700	6.0	1353.5
	290	305	441.5		720	6.1	1343.5
	300	316	451		740	6.2	1333.5
	310	327	461		760	6.3	1314
SNC420	320	337	470.5	Comparatively light	780	6.3	1234.5
	330	347	480.5		800	6.4	1275
	340	350	490.5		820	6.4	1530
	350	363	500		800	6.5	1563
	360	380	505		820	6.6	1608.5
SNC815	370	390	510	Comparatively light	840	6.7	1628
					860	6.8	1628

Fig. 2.22 Material Selection (Reference Screen)

(5) Strength Setting (Dynamic)

Fig. 2.23 shows the metal strength setting screen, on which the user can specify the input torque, speed, and other data.

Description	Symbol	Unit	Pinion	Gear
Torque	T	N m	5.000	8.333
Rotational speed	n	rpm	1000.000	600.000
Life cycles	L	---	10000000	---
Tooth surface roughness	---	Microm	6.000	6.000
Crowning	---	---	Conduct	Conduct
Shaft rigidity and Gear holding	---	---	A Type	---
Lubricating oil coefficient	ZL	---	1.000	---
Over load factor	Ko	---	1.000	---
Root bending strength reliability coefficient	KR	---	1.200	---
Face intensity reliability coefficient	CR	---	1.150	---
Tool diameter influence coefficient	Yc	---	1.150	---

Fig. 2.23 Dynamic Strength Setting

(6) Strength Calculation Result

Fig. 2.24 shows the Metal gear strength calculation result screen.

Description(bending)	Symbol	Unit	Pinion	Gear
Circumferential speed	V	m/s	1.2566	---
Allowable bending stress	σ_{Flim}	N/mm ²	490.5000	284.5000
Tooth form factor	YF	---	2.6846	3.3471
Load distribution coefficient	Yε	---	0.6556	---
Helix angle factor	Yβ	---	1.0000	---
Life factor	KL	---	1.0000	1.0000
Size factor	KFx	---	1.0000	1.0000
Load distribution factor(lead)	KM	---	1.2000	---
Dynamic load factor	KV	---	1.0385	---
Tangential force power	FT	N	490.2314	---
Allowable tangential force	Ftlim	N	1638.9787	762.4947
Tooth root bending stress	σ_F	N/mm ²	146.7124	182.9138
Bending strength(Ftlim/FT)	Sf	---	3.3433	1.5554
Description(pitting)				
Allowable pitting stress	σ_{Hlim}	N/mm ²	1530.0000	1128.0000
Region factor	ZH	---	2.4946	---
Material property factor	ZM	---	60.6000	---
Contact ratio factor	Zε	---	1.0000	---
Life factor	KHL	---	1.0000	1.0000
Roughness factor	ZR	---	0.9201	0.9201
Smooth velocity factor	ZV	---	0.9558	0.9558
Hardness ratio factor	ZW	---	1.0000	1.0000
Load distribution factor	KHβ	---	1.3000	---
Dynamic load factor	CV	---	1.0385	---
Tangential force power	Fc	N	490.2314	---
Allowable tangential force	Fclim	N	554.0296	301.1399
Hertzian stress	σ_H	N/mm ²	1439.2144	1439.2144
Pitting strength(Fc/Hc)	Sfc	---	1.1301	0.6143

Fig. 2.24 Metal Gear Strength Calculation Result Screen

2.15 Gear Accuracy

Fig. 2.25 shows the error tolerance for bevel gears as per the JIS B 1704 standard.

Description	Symbol	Unit	Pinion	Gear
Single pitch deviation (+-)	ft	Micro-m	24	25
Pitch deviation	ftu	Micro-m	31	33
Total cumulative pitch deviation (+-)	Ft	Micro-m	97	100
Radial run-out	fr	Micro-m	33	48

ACCURACY for Gear (JIS B 1704): JAPANESE INDUSTRIAL STANDARDS.

Fig. 2.25 Gear Accuracy

2.16 Sliding Ratio and Hertzian Stress Graphs

Fig. 2.26 and Fig. 2.27 show the sliding ratio and Hertzian stress graphs for a bevel gear pair, respectively.

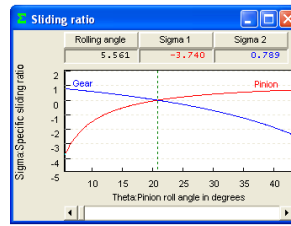


Fig. 2.26 Slipping Ratio Graph

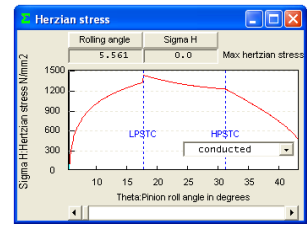


Fig. 2.27 Hertzian Stress Graph

2.17 FEM Tooth Profile Stress Analysis

Stress analysis can be easily performed by simply clicking the [FEM] button after the strength calculation. Fig. 2.28 shows the FEM analysis setting screen. The user may change the Young modulus, Poisson ratio, number of partitions, and load values.

This System supports five types of stresses (δ_x , δ_y , shear stress δ , and principal stresses δ_1 , δ_2). The reliability of a gear pair can be improved by calculating the gear strength and then evaluating the actual stress on the tooth flanks. Fig. 2.29 and Fig. 2.30 show the equivalent stress curves for the maximum (δ_1) and minimum (δ_2) principal stresses, respectively.

Description	Symbol	Unit	Pinion	Gear
Material symbol	---	---	SCM420	SCM440
Elastic modulus	E	MPa	205800.0	205800.0
Poisson ratio	ν	---	0.300	0.300
Height partitions	Vd	---	8	8
Width partitions	Hd	---	22	19
Load point position	Ph	---	2	2
Load	Ft	N	490.231	---
Number of the color tone	nc	---	100	---
Magnification of the displacement	Sd	---	100	---

Fig. 2.28 FEM Analysis Settings

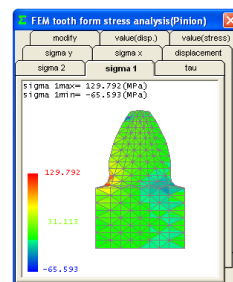


Fig. 2.29 Maximum Principle Stress (δ_1)

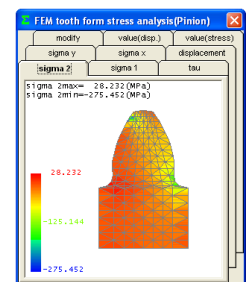


Fig. 2.30 Minimum Principle Stress (δ_2)

2.18 Bearing Load Calculation

The System calculates the loads exerted on both the gear and bearings.

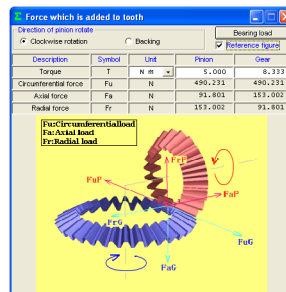


Fig. 2.31 Loads on Gear Tooth Flanks

Description	Symbol	Unit	Pinion	Gear
Distance to center of face width	L	mm	14.3988	10.1997
Bearing span 1	X1	mm	10.000	10.000
Bearing span 2	X2	mm	10.000	10.000
Axial load	Fva	N	91.801	151.002
Radial load which is added to bearing A				
Radial load (Total)	Fvr	N	733.428	696.674
Radial load by Fr	Vr(1)	N	234.203	128.511
Radial load by Ft	Vr(2)	N	486.223	684.233
Radial load by Fa	Vr(3)	N	18.726	92.017
Radial load which is added to bearing B				
Radial load (Total)	Fvr	N	280.440	194.688
Radial load by Fr	Vr(1)	N	81.201	36.720
Radial load by Ft	Vr(2)	N	196.192	194.092
Radial load by Fa	Vr(3)	N	18.726	92.017

Fig. 2.32 Loads on Bearings

2.19 Tooth Profile Measurement

The System produces measurement data that can be used on either Zeiss 3D measuring systems or Osaka Seimitsu Kikai's measuring machines. Specify whichever you prefer when ordering the System.

(1) Outline of Measurement Data for Zeiss 3D Measuring Systems

Fig. 2.33 shows the setting screen for Zeiss 3D measuring systems. Specifying the number of partitions along with the relief amount and standard distance values for measurement causes the System to output the measurement point coordinates and vectors as shown in Fig. 2.34 into a data file.

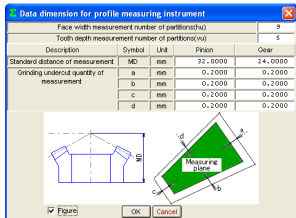


Fig. 2.33 Measurement Data Settings

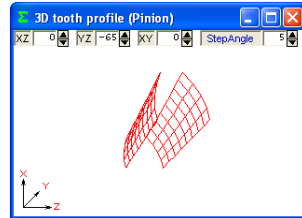


Fig. 2.34 Generated Tooth Profile

2.21 Manufacturing Examples

Fig. 2.37 is an example of a gear set machined using an NC ball-end milling machine with tooth profile data generated by this System. (The tooth profile data was imported into a CAD/CAM system before loading into the NC machine). Fig. 2.38 is a photograph of a photofabricated gear model.



Fig. 2.37 Example of Machined Gear Pair



Fig. 2.38 Photo fabricated Gear Model (m1, NT28, α 20°, β 35°)

(2) Outline of Measurement Data for Osaka Seimitsu Kikai Measuring Machines

Specifying the measuring data as shown in Fig. 2.35 causes the software to output the nominal measurement data into a data file. The manufacturer's catalog says that the measuring machines (HyB-35 and HyB-65) perform "linear" measurement, rather than "point-to-point" measurement, for precision measurement. Unlike the grid-point based measurement used in the 3D measuring systems, these machines linearly measure up to the edge of each tooth to detect subtle profile errors for improved gear accuracy.

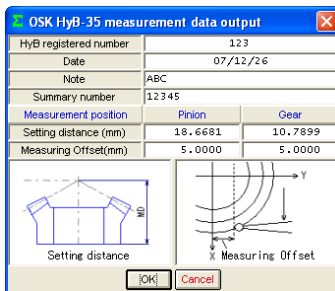


Fig.2.35 Measurement Data Settings

2.20 Ball Height Measurement

Ball height measurement is a technique to control the tooth thickness of a gear, in which the measurement is made with respect to the ball placed around the center of the gear face width. This technique is suitable for controlling the gear tooth thickness in the manufacturing phase. Fig. 2.36 shows how the ball height of a bevel gear is measured.

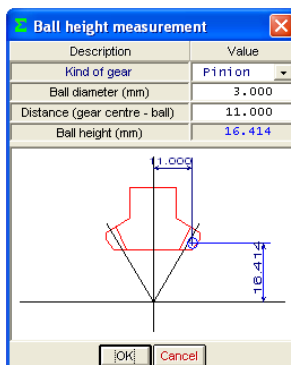


Fig. 2.36 Ball Height Measurement