

**[5] Planetary gear design system  
(Planetary gear and Mechanical paradox gear)**

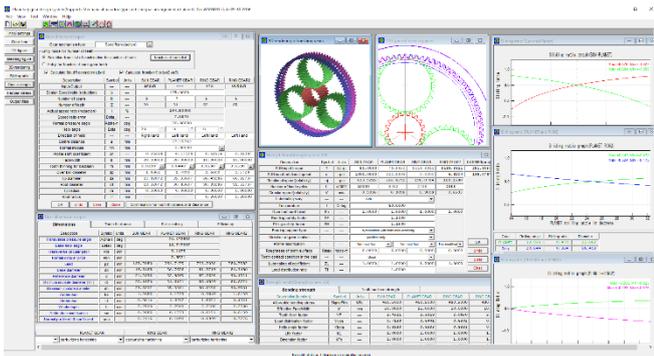


Fig. 5.1 Planetary gear design system

**5.1 Abstract**

This software is a software that can easily design planetary gears and mechanical paradox gears, and can automatically determine the combination of the number of teeth, the center distance, etc., and can easily design the gear dimensions and gear strength. In addition, interference check of planetary gears, profile shift factor calculation, etc. can be easily calculated. Figure 5.1 shows the whole screen of the calculation result.

**5.2 Gear to apply**

- (1) Type : Equal arrangement (Planetary, Solar, Star)
- (2) Material of the gear : Steel, Plastic
- (3) Tooth profile : Involute
- (4) Option : 3K paradox type, Small number of teeth, Double pinion, and Non-equal arrangement

**5.3 Property (Basic rack)**

In the properties, set the tip diameter determination method, basic rack, module or center distance reference, gear accuracy and friction coefficient. Figure 5.2 shows the property screen.

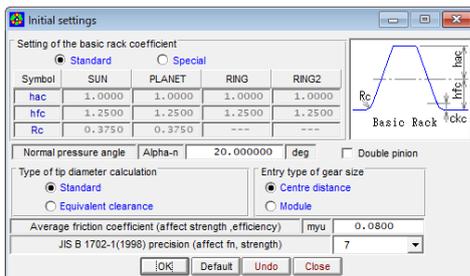


Fig. 5.2 Property (basic rack)

**5.4 Selection of planetary gear mechanism**

Select the planetary gear type shown in Figure 5.3.

- (1) The number of planet gears is 1 to 21.
- (2) The number of teeth can be selected from the method of direct input or the number of teeth list calculated from the speed ratio (Fig. 5.5).

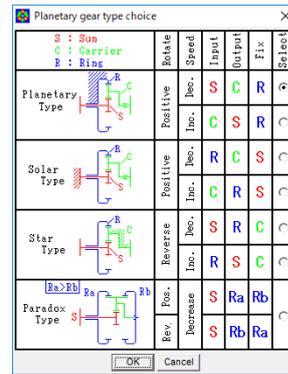


Fig. 5.3 Type of planetary gear

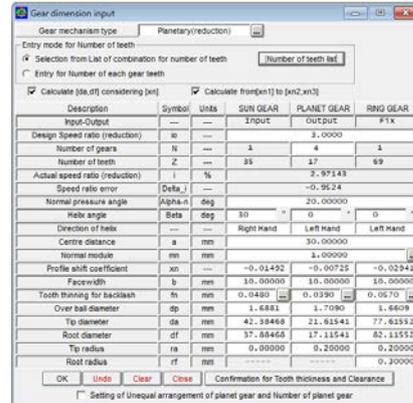


Fig. 5.4 Gear specification (input)

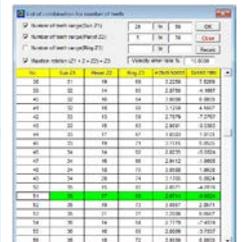


Fig. 5.5 teeth list

- (3) You can calculate module distance from center distance or center distance from module.
- (4) The calculation of the profile shift factor is performed so that the backlash becomes zero from the module and the center distance.
- (5) The default value of thinning for backlash is 1/2 of the JIS backlash standard middle value.
- (6) The tip circle diameter is calculated from the basic rack and dislocation coefficient set in the property, but it can be changed.
- (7) The shape of the tooth root of the external gear is a trochoid based on the basic rack. The tooth root of the internal gear is the input R connection.
- (8) Gear tips can be created with a single R.
- (9) Changing one profile shift factor changes the remaining ones in tandem, but you can enter each gear individually. The tooth shape can be confirmed by confirming the tooth thickness and the crest in Fig. 5.6. You can also check the tooth profile and clearance after changing the profile shift factor and tip diameter on this screen. The tooth shape at this point is only the tooth surface, and the root shape is not included.

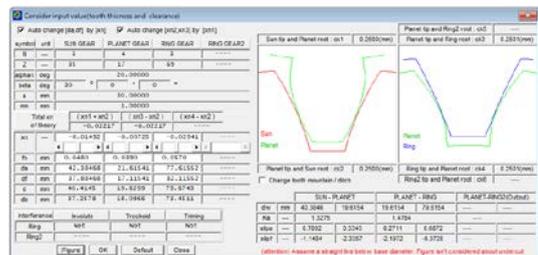


Fig.5.6 Support of the dimension

### 5.5 Gear dimension

The various calculation results are shown in Fig. 5.7 to Fig. 5.10. On this screen, you can check the interference, efficiency, clearance and backlash.

Dimensions		Tooth thickness		Pair meshing		Efficiency	
Description	Symbol	Units	SUN GEAR	PLANET GEAR	RING GEAR		
Transverse pressure angle	Alpha-t	deg				22.795877	
Base helix angle	Betab	deg				28.024321	
Transverse circular pitch	Pbt	mm				3.3443	
Normal circular pitch	Pbn	mm				2.9521	
Lead	pz	mm	219.9115	106.8142		433.5398	
Base diameter	db	mm	37.2578	18.0966		73.4511	
Reference diameter	d	mm	40.4145	19.6299		79.6743	
Minimum involute diameter (Tf)	dt	mm	38.6593	18.2424		77.8816	
Maximum involute diameter	dh	mm	42.3847	21.4269		81.7775	
Addendum	ha	mm	0.9851	0.9928		1.0294	
Dedendum	hf	mm	1.2649	1.2572		1.2206	
Whole depth	h	mm	2.2500	2.2500		2.2500	
Addendum modification	xm	mm	-0.0149	-0.0073		-0.0294	
Normal profile shift coefficient	xnc	---	-0.0851	-0.0643		0.0539	

Fig.5.7 Result (Gear dimension)

Dimensions		Tooth thickness		Pair meshing		Efficiency	
Description	Symbol	Units	SUN GEAR	PLANET GEAR	RING GEAR		
Normal tooth thickness	sn	mm	1.5089	1.5240		1.5315	
Transverse tooth thickness	st	mm	1.7423	1.7598		1.7685	
Number of teeth spanned	zm	---	6	3		12	
Base tangent length(standard)	W	mm	16.9637	7.7334		35.3827	
Base tangent length(Design)	W'	mm	16.9157	7.6944		35.4397	
Measuring ball diameter	dp	mm	1.6881	1.7090		1.6609	
Measurement over balls(standard)	dm	mm	42.6297	21.8687		77.3801	
Measurement over balls(Design)	dm'	mm	42.4983	21.7696		77.5533	
Caliper depth	Hj	mm	0.9964	1.0162		1.0253	
Caliper tooth thickness(standard)	Sj	mm	1.5597	1.5646		1.5921	
Caliper tooth thickness(Design)	Sj'	mm	1.5087	1.5233		1.5221	

Fig.5.8 Result (Tooth thickness)

Dimensions		Tooth thickness		Pair meshing		Efficiency	
Description	Symbol	Units	SUN GEAR	PLANET GEAR	RING GEAR		
Operating transverse pressure	Alpha-wt	deg	22.6947			22.6947	
Operating helix angle	betaw	deg	29.9816			29.9816	
Operating pitch diameter	dw	mm	40.3846	19.6154	19.6154	79.6154	
Operating facewidth	bw	mm	10.0000			10.0000	
Clearance	ck	mm	0.2500	0.2500	0.2501	0.2501	
Contact length	ga	mm	4.2652			4.3641	
Near transverse contact ratio	Ka1	---	0.5838			0.7212	
Far transverse contact ratio	Ka2	---	0.6916			0.5838	
Transverse contact ratio	Ka	---	1.2754			1.3050	
Overlap ratio	Kb	---	1.5915			1.5915	
Total contact ratio	Kc	---	2.8669			2.8965	
Sliding ratio at tip	Sltpa	---	0.7002	0.5057	0.2585	0.5898	
Sliding ratio at root	Sltpf	---	-1.0229	-2.3357	-1.3245	-0.3450	
Transverse backlash	jnt	mm	0.0986			0.1088	
Backlash angle	Jtheta	deg	0.3031	0.6241	0.6887	0.1697	
Total backlash angle(input axis)	Jtheta'	deg		0.6376 (Sun)			
Maximum contact diameter	dja	mm	42.3847	21.4269	21.4269	81.2018	
Minimum contact diameter	djf	mm	39.0446	18.3343	18.3036	77.8816	

Fig.5.9 Result (Pair meshing)

Dimensions		Tooth thickness		Pair meshing		Efficiency	
Rotate ratio		SUN	PLANET	RING	CARRIER		
		1.0000	-1.0294	0.0000	0.3365		
Efficiency		0.9880					
RING GEAR interference							
Description	RING						
Involute		Not occurrence					
Trochoid		Not occurrence					
Trimming		Not occurrence					
Clearance(mm)							
Sun tip and Planet root		0.2500 (mm)					
Planet tip and Sun root		0.2500 (mm)					
Planet tip and Ring root		0.2501 (mm)					
Ring tip and Planet root		0.2501 (mm)					

Fig.5.10 Result (Efficiency, etc.)

### 5.6 Tooth profile figure

#### 5.6.1 Tooth profile (2D)

The meshing of the gears is displayed in a two-dimensional view as shown in Figure 5.11 and Figure 5.12. Since the auxiliary circle and the common normal can be displayed by the operation screen, it is easy to check the contact position of the tooth surface. You can change the rotation angle of the gear to zoom in.

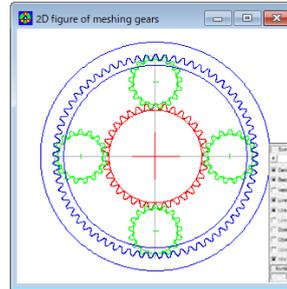


Fig.5.11 Meshing of the tooth profile

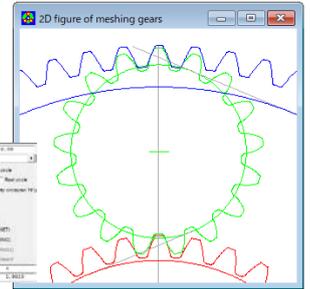


Fig.5.12 Zoom

#### 5.6.2 Meshing of a pair tooth profile (2D)

The meshing of one tooth can be confirmed in the two-dimensional view of Fig. 5.13. On this screen, you can check the interference between the internal gear and external gear teeth and the tooth base in more detail. You can change the rotation angle of the gear to zoom in.

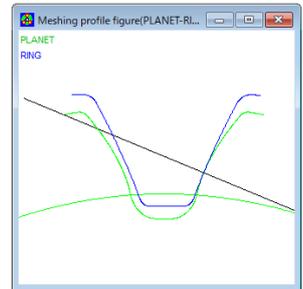
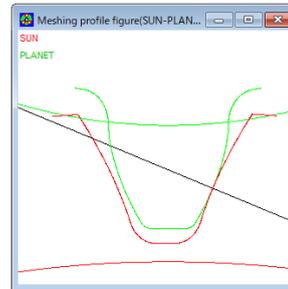


Fig. 5.13 Meshing of a pair tooth profile (2D)

#### 5.6.3 rendering

Gear mesh can be displayed in a three-dimensional view as shown in Figure 5.14 and Figure 5.15. In addition, a control form that can be rotated in the X, Y, and Z directions is shown in Figure 5.16.

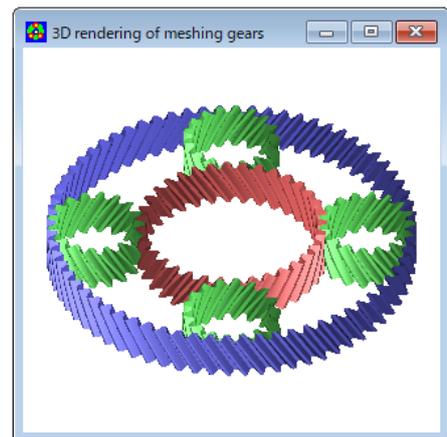


Fig.5.14 Teeth rendering

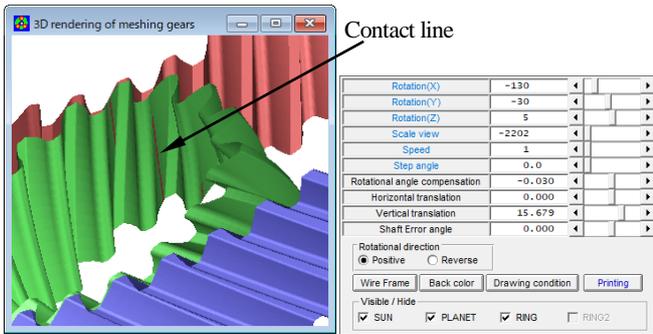


Fig.5.15 profile (Zoom)

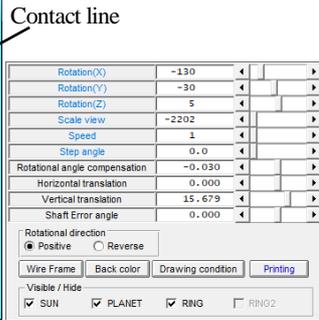
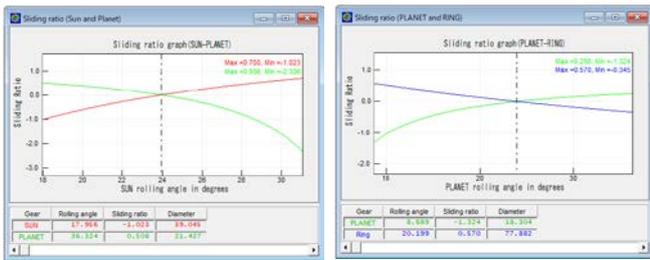


Fig.5.16 Control form

### 5.7 Sliding ratio graph

The sliding ratio graph is shown in Fig. 5.17 and Fig. 5.18.



(Sun × Planet)

(Planet × Internal)

Fig.5.17 sliding ratio graph1 Fig5.18 sliding ratio graph2

### 5.8 Gear strength

#### 5.8.1 Initial settings for gear strength calculation

You can select metal material and plastic on the strength initial setting screen shown in Fig. 5.19. Select the allowable stress  $\sigma_{Flim}$  and  $\sigma_{Hlim}$  from Fig. 5.20. Note that  $\sigma_{Flim}$  and  $\sigma_{Hlim}$  can be input arbitrary numbers. The torque unit can be selected from N·m, N·cm, kgf·m, kgf·cm and gf·cm.

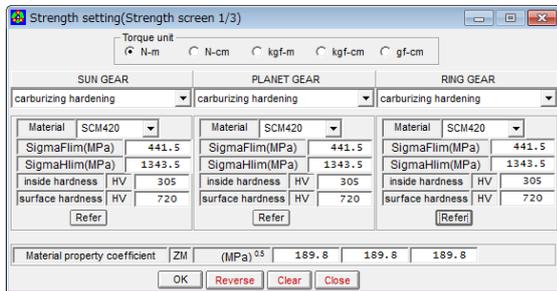


Fig.5.19 Input (Material)

Structural alloy steel	Centerhardness		$\sigma_{Flim}$ MPa	Effective carburizing	Tooth surface hardness		$\sigma_{Hlim}$ MPa
	HB	HV			HV	HRc	
SCM415	220	231	333.5	Comparatively light	5.80	5.4	1284.5
	230	242	353		6.00	5.5	1314
	240	252	372.5		6.20	5.6	1343.5
	250	263	392.5		6.40	5.7	1383.5
	260	273	402		6.60	5.9	1393.5
SCM420	270	284	417		6.80	5.9	1383.5
	280	295	431.5		7.00	6.0	1393.5
	290	305	441.5		7.20	6.1	1343.5
	300	316	451		7.40	6.2	1333.5
	310	327	461		7.60	6.3	1314
SNC420	320	337	470.5	7.80	6.3	1294.5	
	330	347	481.5	8.00	6.4	1275	
	340	358	490.5	5.80	5.4	1530	
SNC815	350	369	500	6.00	5.5	1589	
	360	380	505	6.20	5.6	1608.5	
	370	390	510	6.40	5.7	1628	

Fig.5.20 Example of the allowable stress of the steel

### 5.8.2 Strength specification input

Enter various values in the strength specification input screen shown in Fig. 5.21. The torque and rotational speed can be set by either input side or output side.

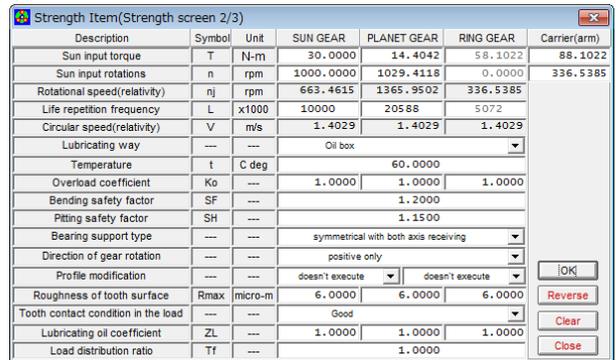


Fig.5.21 Input (Gear strength dimension)

### 5.8.3 Strength calculation result

The intensity calculation result screen is displayed in Fig. 5.22 and Fig. 5.23. The strength calculation also takes into account the efficiency and meshing ratio. The metal gears are subjected to strength calculation based on JGMA 401-01: 1974, JGMA 401-02: 1975. Moreover, the stress value of the resin material adopts the experimental value of the material in consideration of the temperature, life and so on.

Bending strength		Tooth surface strength	
Description (bending)	Symbol	Unit	
Allowable bending stress	SigmaFlim	MPa	441.5000
Effective Face/Width	b'	mm	10.0000
Tooth form factor	YF	---	2.4262
Load distribution factor	Yeps	---	0.8281
Helix angle factor	Ybeta	---	0.7500
Life factor	KL	---	1.0000
Dimension factor	KFx	---	1.0000
Dynamic load factor	Kv	---	1.0403
Speed correction factor	KVo	---	---
Temperature factor	KT	---	---
Lubrication factor	KLo	---	---
Material factor	KM	---	---
Call circumference force	Ft	N	371.4286
Allowable circumference force	Ftlim	N	2347.1505
Bending strength	Sft	---	6.3193
Bending stress	SigmaF	MPa	69.8659

Fig.5.22 Gear strength calculation result (Bending)

Bending strength		Tooth surface strength	
Description (pitting)	Symbol	Unit	
Allowable tooth surface stress	SigmaHlim	MPa	1343.5000
Effective Face/Width	bw	mm	10.0000
Zone factor	ZH	---	2.2288
Material property coefficient	ZM	(MPa) <sup>0.5</sup>	189.8000
Contact ratio factor	Zeps	---	0.9100
Life factor	KHL	---	1.0000
Roughness factor	ZR	---	0.9204
Smooth velocity factor	ZV	---	0.9581
Hardness ratio factor	ZW	---	1.0000
Load distribution factor	KHbeta	---	1.0000
Dynamic load factor	Kv	---	1.0404
Young modulus	E	---	---
Call circumference force	Fc	N	371.1537
Allowable circumference force	Fclim	N	909.7035
Tooth surface strength	sfc	---	2.4510
Tooth surface (Hertz) stress	SigmaH	MPa	858.1527

Fig.5.23 Gear strength calculation result (Pitting)

### 5.9 Hertz stress graph

Hertz stress graphs are shown in Figure 5.24 and Figure 5.25.

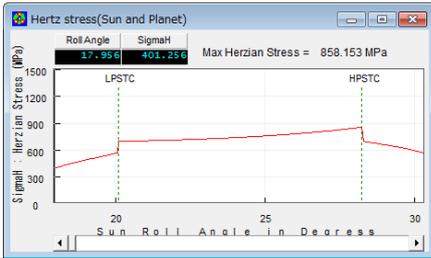


Fig.5.24 Hertzian stress (Sun)

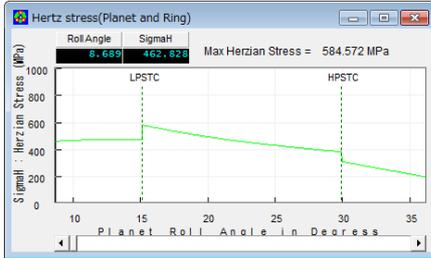


Fig.5.25 Hertzian stress (Planet)

### 5.10 Other

- 1) Tooth profile data of gears can be output.
  - DXF file : 2D, 3D All teeth meshing
  - IGES file : 3D(Tooth)
  - TEXT file : 2-dimensional tooth profile coordinate
- 2) You can print dimensional calculation results, strength calculation results, 2D tooth profiles, slip ratio graphs, and Hertz stress graphs.
- 3) You can save and load design data.

### 5.11 Mechanical paradox gears (3K type)

A Mechanical paradox gears using a total of four gears of the sun, planets, and two internal teeth is well known. Mechanical paradox gears are very computationally expensive, but can be easily designed using this software. The input is for the sun gear, the fixed for the internal gear 1, and the output for the internal gear 2 type 3K type only.

The number of teeth of internal gear 1 and internal gear 2 determines the same direction deceleration and the reverse direction deceleration. The design example is shown below.

#### 5.11.1 Specification of gear specifications

- 1) In Properties, select module criteria.
- 2) Select the 3K type in Figure 5.3 and proceed to the mechanical paradox gears in Figure 5.26.
- 3) Input the design reduction ratio as 135 and the number of planet gears as three.
- 4) Display the tooth number list screen, and select the combination of the number of teeth that seems appropriate. (See Figure 5.27)

As selection conditions at this time,

- (a) Difference between the actual speed ratio and the design speed ratio error.
- (b) The number of teeth must be correct.

Here we choose  $z_1=20, z_2=31, z_3=82, z_4=85$  as an example.

- (5) Then press the Tab key and enter  $\alpha=20, \beta=20, m_n=1$  in order. When the module is entered, the standard center distance, profile shift factor, tip circle diameter and root circle diameter are determined based on the basic rack in Figure 5.2.
- (6) The theoretical center distance is 27.6686 mm, but it can be changed according to the purpose. Fig. 5.26 shows the gear specification screen.
- (7) Once the center distance and module have been determined, you can change the tooth height and tooth thickness. On this screen (Fig.5.28), you can change the profile shift factor and tip diameter while checking the tooth profile. Check the contact of the teeth, interference with the teeth, clearance and internal gear.

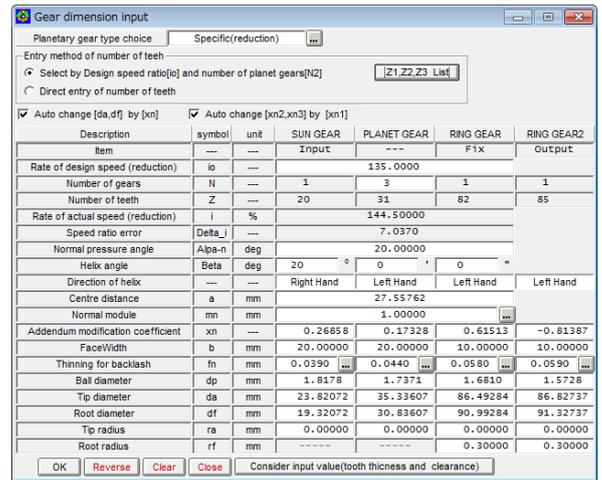


Fig.5.26 Input of gear dimension



Fig.5.27 The number of teeth list

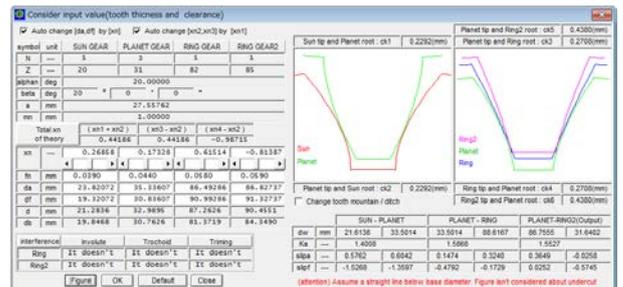


Fig.5.28 Input support screen

- (8) Check the efficiency, meshing ratio and slip ratio on the dimension calculation result screen as shown in Figure 5.29-5.32. The efficiency of

the mechanical paradox gears in this example is 73.1% as shown in Figure 5.32.

(9) Also, check how much the interference between the external gear and the internal gear can actually be secured by one tooth engagement.

(10) In the case of the example, the dimensions of module 1 have been determined, but it may be necessary to change the size by strength calculation. In that case, change the tooth width or increase the module distance, center distance and tip diameter, etc. The strength calculation should be done carefully as the ratio of torque increases as the rotation ratio increases.

Standard		Thickness		Pair meshing		Others	
Description	symbol	unit	SUN GEAR	PLANET GEAR	RING GEAR	RING GEAR2	
Transverse pressure angle	at	deg			21.172832		
Base helix angle	Betab	deg			18.747237		
Transverse circular pitch	Pbt	mm			3.1175		
Normal circular pitch	Pbn	mm			2.9521		
Lead	Lead	mm	183.7080	284.7475	753.2030		780.7592
Base diameter	db	mm	19.8468	30.7626	81.3719		84.3490
Reference pitch diameter	d	mm	21.2836	32.9895	87.2626		90.4551
Minimum validity diameter (TF)	dt	mm	20.1670	31.6121	86.4929		86.8274
Maximum validity diameter	dh	mm	23.8207	35.3361	90.6558		90.9501
Addendum	ha	mm	1.2686	1.1733	0.3849		1.8139
Dedendum	hf	mm	0.9814	1.0767	1.8651		0.4361
Whole depth	h	mm	2.2500	2.2500	2.2500		2.2500
Addendum modification	xm	mm	0.2686	0.1733	0.6151		-0.8139
Normal profile shifted coefficient	xnc	---	0.2116	0.1090	0.6999		-0.7276

Fig.5.29 Result (Gear dimension)

Standard		Thickness		Pair meshing		Others	
Description	symbol	unit	SUN GEAR	PLANET GEAR	RING GEAR	RING GEAR2	
Normal tooth thickness	sn	mm	1.7248	1.6501	1.0613		2.1005
Transverse tooth thickness	st	mm	1.8355	1.7560	1.1294		2.2353
Number of teeth spanned	zm	---	4	5	12		10
Base tangent length(standard)	W	mm	10.8506	13.9215	35.7414		28.9098
Base tangent length(Design)	W'	mm	10.8116	13.8775	35.7994		28.9688
Measuring ball diameter	dp	mm	1.8178	1.7371	1.6810		1.5728
Dimension over balls(standard)	dm	mm	24.4103	35.6976	86.1985		86.7829
Dimension over balls(design)	dm'	mm	24.3235	35.5879	86.3598		86.9894
Caliper depth	Hj	mm	1.3009	1.1925	0.3835		1.8050
Caliper tooth thickness(standard)	Sj	mm	1.7647	1.6964	1.1230		2.1631
Caliper tooth thickness(design)	Sj'	mm	1.7234	1.6496	1.0573		2.0963

Fig.5.30 Result (Tooth thickness)

Standard		Thickness		Pair meshing		Others	
Description	symbol	unit	SUN GEAR	PLANET GEAR	RING GEAR	PLANET And RING2	
Operating transverse pressure	awt	deg	23.3289		23.3289		13.5267
Operating helix angle	betaw	deg	20.2852		20.2852		19.2433
Operating pitch diameter	dw	mm	21.6138	33.5014	33.5014	88.6167	86.7555 31.6402
Operating Facewidth	bw	mm	20.0000		10.0000		10.0000
Clearance	ck	mm	0.2292	0.2292	0.2708	0.4380	0.4380
Contact length	ga	mm	4.3669		4.9469		4.8405
Near transverse contact ratio	Ka1	---	0.6608		0.9260		1.6016
Far transverse contact ratio	Ka2	---	0.7400		0.6608		-0.0490
Transverse contact ratio	Ka	---	1.4008		1.5868		1.5527
Overlap ratio	Kb	---	2.1774		1.0887		1.0887
Total contact ratio	Kc	---	3.5781		2.6755		2.6434
Sliding ratio at tip	Slipa	---	0.5762	0.6042	0.1474	0.3240	-0.0258 0.3649
Sliding ratio at root	Slipf	---	-1.5268	-1.3597	-0.4792	-0.1729	-0.5745 0.0252
Transverse backlash	jnt	mm	0.0876		0.1077		0.1088
Backlash angle	βStα	deg	0.5061	0.3265	0.4012	0.1517	0.1478 0.4052
Total backlash angle(input axis)	βStα'	deg			1.1341 (Sun)		
Maximum contact diameter	dja	mm	23.8207	35.3361	35.3361	90.3275	35.3361 89.6187
Minimum contact diameter	dja'	mm	20.3372	31.9564	31.6620	86.4928	31.7130 86.8274

Fig.5.31 Result (Pair meshing)

Standard		Thickness		Pair meshing		Others	
Rotate ratio							
SUN	PLANET	RING	CARRIER	RING2			
1.0000	-0.3226	0.0000	0.1961	0.0069			
Efficiency 0.7155							
RING GEAR interference							
Description	RING	RING2					
Involute	It doesn't	It doesn't					
Trochoid	It doesn't	It doesn't					
Trimming	It doesn't	It doesn't					
Clearance(mm)							
Sun tip and Planet root	0.2292(mm)						
Planet tip and Sun root	0.2292(mm)						
Planet tip and Ring root	0.2708(mm)						
Ring tip and Planet root	0.2708(mm)						
Planet tip and Ring2 root	0.4380(mm)						
Ring2 tip and Planet root	0.4380(mm)						

Fig.5.32 Result (Efficiency, etc.)

### 5.11.2 Tooth profile (2D)

The meshing figure is shown in Fig. 5.33. In the enlarged view of Fig. 5.34, it can be clearly seen that the planetary gear is engaged with the two internal gears. In addition, you can observe the state of the meshing rotation of the strange planet by the tooth profile rendering shown in Fig. 5.35.

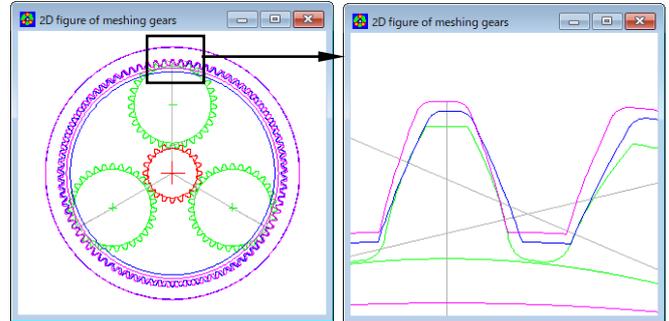


Fig.5.33 Meshing tooth profile

Fig. 5.34 Zoom

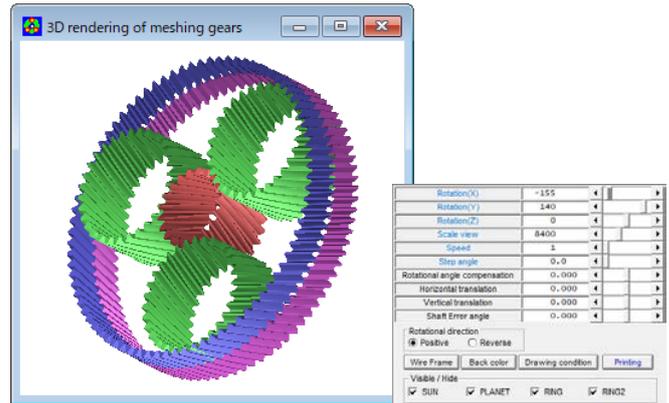


Fig.5.35 Teeth rendering (Gear ratio=135)

### 5.11.3 Mechanical paradox gears example (spur gear)

- (1) Gear strength calculation, sliding ratio and Hertz stress graph can be calculated in the same way as planetary gears.
- (2) Figure 5.36 shows an example of drawing a mechanical paradox gears with a spur gear.

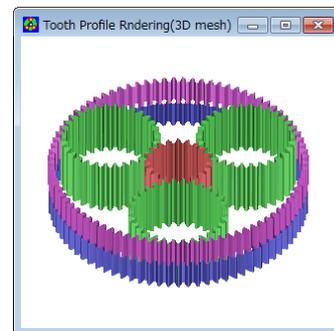


Fig.5.36 Teeth rendering (Spur gear, Gear ratio=93.8)

### 5.12 Small number of teeth (optional)

You can design a planetary gear with 4 or fewer teeth. In the case of a small number of teeth, it is necessary to increase the helix angle because the contact ratio decreases. The following is an example of drawing a planetary gear with 1 sun gear, 1 planet gear and 2 internal gear teeth.

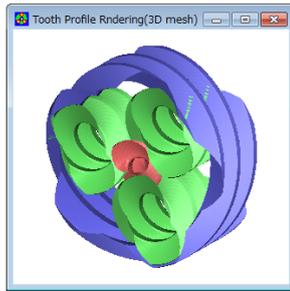
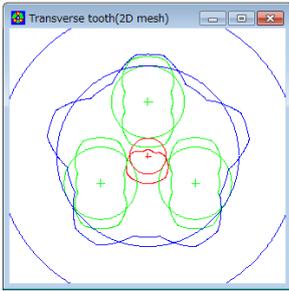


Fig.5.37 Teeth profile(2D) Fig.5.38 Teeth profile (3D)

5.13 Double pinion (option)

Set the double pinion in Figure 5.2 Properties. The design example is shown below.

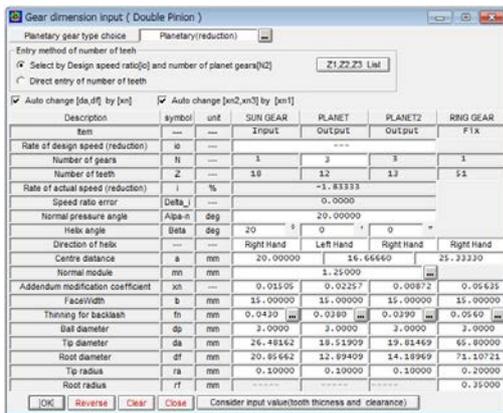


Fig.5.39 Input dimension

Description	symbol	unit	SUN GEAR	PLANET GEAR	PLANET GEAR2	RING GEAR
Transverse pressure angle	awt	deg	21.5114	21.5114	21.5114	21.5114
Base helix angle	betaw	deg	20.0431	20.0430	20.0430	20.0430
Transverse circular pitch	Pwt	mm	3.8969			
Normal circular pitch	Pbn	mm	3.6902			
Lead	Lead	mm	206.6716	137.7810	149.2628	585.5694
Base diameter	db	mm	22.3277	14.8851	16.1255	65.2617
Reference pitch diameter	d	mm	23.9440	15.9627	17.2929	67.8413
Minimum validity diameter (TF)	dt	mm	22.3968	14.8937	16.1289	66.0833
Maximum validity diameter	dt	mm	24.3877	16.4364	19.7292	70.7173
Addendum	ha	mm	3.2498	1.2782	1.2609	3.0207
Dedendum	hf	mm	1.5437	1.5183	1.5156	1.6329
Whole depth	h	mm	3.8135	2.8135	3.8135	3.6536
Addendum modification	xm	mm	0.0188	0.0282	0.0109	0.0704
Normal profile shifted coefficient	yn		-0.0352	-0.0219	-0.0369	0.1218

Fig.5.40 Result (Gear dimension)

Description	symbol	unit	SUN GEAR	PLANET GEAR	PLANET GEAR2	PLANET2 And RING
Operating transverse pressure	awt	deg	21.5114	21.5148	21.5148	21.5152
Operating helix angle	betaw	deg	20.0431	20.0430	20.0430	20.0430
Operating pitch diameter	dwt	mm	24.0000	18.0000	18.9999	17.3333
Operating facewidth	dw	mm	15.0000	15.0000	15.0000	15.0000
Clearance	ca	mm	0.3121	0.3121	0.3122	0.4719
Contact length	ga	mm	5.5358	5.0503	5.4226	5.4226
Near transverse contact ratio	Ka1		0.6428	0.6428	0.6428	0.6428
Far transverse contact ratio	Ka2		0.6761	0.6429	0.6429	0.7487
Transverse contact ratio	Ka		1.3179	1.2897	1.2895	1.3915
Overlap ratio	kb		1.3564	1.3564	1.3564	1.3564
Total contact ratio	Kc		2.6243	2.5921	2.5921	2.6979
Sliding ratio at tip	Slipw		0.9353	0.7876	0.8857	0.8183
Sliding ratio at root	Slipr		-3.2032	-14.4604	-11.2250	-7.7519
Transverse backlash	jt	mm	0.0855	0.0813	0.0813	0.1003
Backlash angle	beta	deg	0.4390	0.6885	0.6290	0.5779
Total backlash angle(input axis)	betaT	deg			2.3742 (Gup)	
Maximum contact diameter	dca	mm	26.3877	18.4384	18.4384	19.7292
Minimum contact diameter	dca	mm	22.6474	14.8976	14.8988	16.1340

Fig.5.41 Result (Tooth thickness)

Description	symbol	unit	SUN GEAR	PLANET GEAR	PLANET GEAR2	PLANET2 And RING
Operating transverse pressure	awt	deg	21.5114	21.5148	21.5148	21.5152
Operating helix angle	betaw	deg	20.0431	20.0430	20.0430	20.0430
Operating pitch diameter	dwt	mm	24.0000	18.0000	18.9999	17.3333
Operating facewidth	dw	mm	15.0000	15.0000	15.0000	15.0000
Clearance	ca	mm	0.3121	0.3121	0.3122	0.4719
Contact length	ga	mm	5.5358	5.0503	5.4226	5.4226
Near transverse contact ratio	Ka1		0.6428	0.6428	0.6428	0.6428
Far transverse contact ratio	Ka2		0.6761	0.6429	0.6429	0.7487
Transverse contact ratio	Ka		1.3179	1.2897	1.2895	1.3915
Overlap ratio	kb		1.3564	1.3564	1.3564	1.3564
Total contact ratio	Kc		2.6243	2.5921	2.5921	2.6979
Sliding ratio at tip	Slipw		0.9353	0.7876	0.8857	0.8183
Sliding ratio at root	Slipr		-3.2032	-14.4604	-11.2250	-7.7519
Transverse backlash	jt	mm	0.0855	0.0813	0.0813	0.1003
Backlash angle	beta	deg	0.4390	0.6885	0.6290	0.5779
Total backlash angle(input axis)	betaT	deg			2.3742 (Gup)	
Maximum contact diameter	dca	mm	26.3877	18.4384	18.4384	19.7292
Minimum contact diameter	dca	mm	22.6474	14.8976	14.8988	16.1340

Fig.5.42 Result (Pair meshing)

Standard	Thickness	Pair meshing	Others
Rotate ratio			
SUN	PLANET	PLANET2	CARRIER
1.0000	-2.8636	1.5944	-0.5455
			RING
			0.0000
Efficiency	0.9248		
RING GEAR interference			
Description	RING		
Involute	It doesn't		
Trochoid	It doesn't		
Triming	It doesn't		
Clearance(mm)			
Sun tip and Planet root	0.3121 (mm)		
Planet tip and Sun root	0.3121 (mm)		
Planet tip and Ring root	0.3122 (mm)		
Ring tip and Planet root	0.3122 (mm)		
Planet tip and Ring2 root	0.3130 (mm)		
Ring2 tip and Planet root	0.4719 (mm)		

Fig.5.43 Result (Efficiency, etc.)

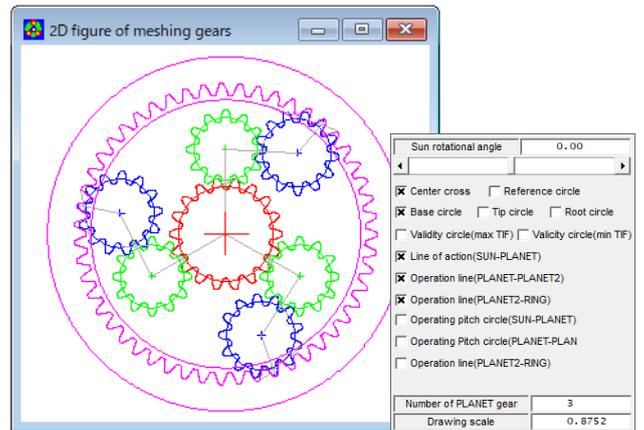


Fig.5.44 Meshing of the tooth profile (2D)

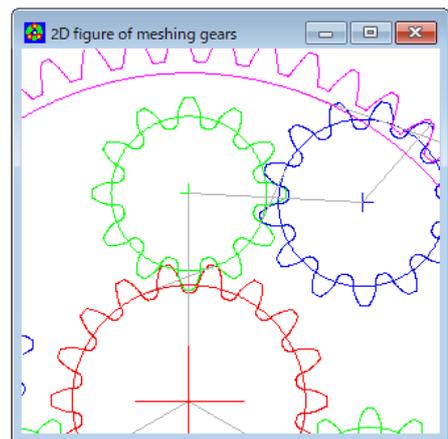


Fig.5.45 Meshing of the tooth profile (Zoom)

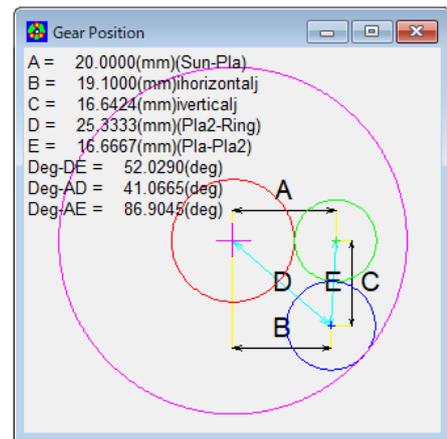


Fig.5.46 Configuration of the gear

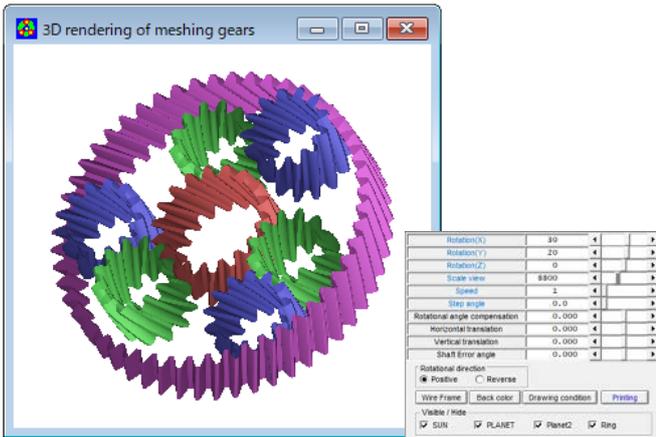


Fig.5.47 Teeth rendering

Description	Symbol	Unit	SUN GEAR	PLANET GEAR	PLANET GEAR2	RING GEAR	Carrier/arm	
Sun input torque	T	N-m	100.0000	65.3843	69.2901	269.5505	169.5505	
Sun input rotations	n	rpm	1000.0000	2863.6364	1594.4056	0.0000	545.4545	
Rotational speed(velocity)	nj	rpm	1545.4545	2318.1818	2139.8601	545.4545		
Life repetition frequency	L	x1000	10000	15000	13846	3529		
Circular speed(velocity)	V	m/s	1.9421	1.9421	1.9421	1.9421		
Lubricating way			Gis					
Temperature	t	C deg	60.0000					
Overload coefficient	Ko		1.0000	1.0000	1.0000	1.0000		
Bending safety factor	SF		1.2000					
Pitting safety factor	SH		1.1500					
Bearing support type			symmetrical with both axis receiving					
Direction of gear rotation			positive only					
Profile modification			doesn't execute	doesn't execute	doesn't execute	doesn't execute	OK	
Roughness of tooth surface	Rmax	micro-m	6.0000	6.0000	6.0000	6.0000	Reverse	
Tooth contact condition in the load			Good					
Lubricating oil coefficient	ZL		1.0000	1.0000	1.0000	1.0000	Clear	
Load distribution ratio	Tf		1.0000					Close

Fig.5.48 Gear strength (Bending)

Bending strength		Tooth surface strength				
Description(bending)	Symbol	Unit	SUN GEAR	PLANET GEAR	PLANET GEAR2	RING GEAR
Allowable bending stress	SigmaFm	MPa	441.5000	441.5000	441.5000	441.5000
Effective FaceWidth	b'	mm	15.0000	15.0000	15.0000	15.0000
Tooth form factor	YF		2.8091	3.2102	3.1421	2.0660
Load distribution factor	Yeps		0.7588	0.7778	0.7778	0.7184
Helix angle factor	Ybeta		0.8333	0.8333	0.8333	0.8333
Life factor	KL		1.0000	1.0000	1.0000	1.0000
Dimension factor	KDx		1.0000	1.0000	1.0000	1.0000
Dynamic load factor	Kv		1.0942	1.0942	1.0942	1.0942
Speed correction factor	KVv					
Temperature factor	KT					
Lubrication factor	KLv					
Material factor	KM					
Call circumference force	Fl	N	2777.7779	2724.3567	2665.0146	2642.6557
Allowable circumference force	Flim	N	3349.4064	3030.0017	3095.6166	5097.9676
Bending strength	Sfl		1.2778	1.1122	1.1616	1.9291
Bending stress	SigmaF	MPa	345.5194	386.8648	380.0871	338.8635

Fig.5.49 Gear strength (Pitting)

Tooth profile data file output and sliding ratio graph, etc. are equal to the basic software.

### 5.14 Non-equality position of planet gear (Option)

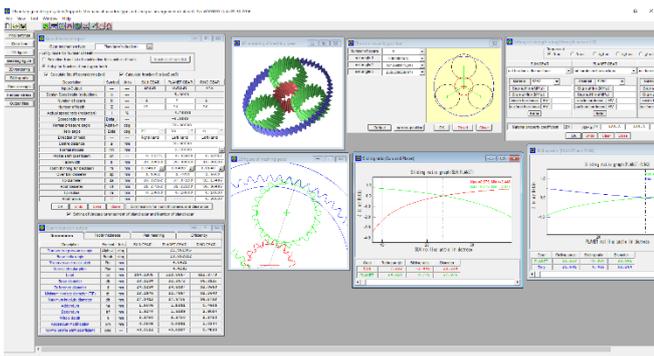


Fig.5.50 Non-equality position of planet gear

The design example of the planetary type (deceleration) nonuniform layout is shown below. In the case of Fig. 5.51, the number of sun teeth is 15, the number of planet teeth is 21, and the number of internal gear teeth is 57 under the condition of equal arrangement. If the number of internal gear teeth is 56, it can be calculated by setting the unequal arrangement shown in Fig. 5.51.

Description	symbol	unit	SUN GEAR	PLANET GEAR	RING GEAR
Rate of design speed (reduction)	lo			5.0000	
Number of gears	N		1	3	1
Number of teeth	Z		15	21	57
Rate of actual speed (reduction)	i	%		4.80000	
Speed ratio error	Delta_i			-4.0000	
Normal pressure angle	Alpa-n	deg		20.00000	
Helix angle	Beta	deg	0	0	0
Direction of helix					
Centre distance	a	mm		33.00000	
Normal module	mm	mm		1.80000	
Addendum modification coefficient	xn		0.20724	0.14802	0.50328
FaceWidth	b	mm	20.00000	20.00000	20.00000
Thinning for backlash	fn	mm	0.0470	0.0510	0.0670
Ball diameter	dp	mm	3.0000	3.0000	3.0000
Tip diameter	da	mm	31.34606	41.93287	100.81181
Root diameter	df	mm	23.24606	33.83287	108.91181
Tip radius	ra	mm	0.00000	0.00000	0.00000
Root radius	rf	mm			0.41250

Fig.5.51 Equality position of planet gear

The input screen with the number of internal gear teeth changed to 56 is shown in Figure 5.52. The module has  $m_n = 1.5$  as in Figure 5.51, so the internal gear profile shift factor is slightly larger. The input screen with the number of internal gear teeth changed to 56 is shown in Figure 5.52. The module has  $m_n = 1.5$  as in Figure 5.51, so the internal gear profile shift factor is slightly larger. Figures 5.53 to 5.55 show the dimension results.

Description	symbol	unit	SUN GEAR	PLANET GEAR	RING GEAR
Rate of design speed (reduction)	lo			5.0000	
Number of gears	N		1	3	1
Number of teeth	Z		15	21	56
Rate of actual speed (reduction)	i	%		4.73333	
Speed ratio error	Delta_i			-5.3333	
Normal pressure angle	Alpa-n	deg		20.00000	
Helix angle	Beta	deg	0	0	0
Direction of helix					
Centre distance	a	mm		33.00000	
Normal module	mm	mm		1.80000	
Addendum modification coefficient	xn		0.20724	0.14802	1.11125
FaceWidth	b	mm	20.00000	20.00000	20.00000
Thinning for backlash	fn	mm	0.0470	0.0510	0.0670
Ball diameter	dp	mm	3.0000	3.0000	3.0000
Tip diameter	da	mm	31.34606	41.93287	101.20050
Root diameter	df	mm	23.24606	33.83287	109.30050
Tip radius	ra	mm	0.00000	0.00000	0.00000
Root radius	rf	mm			0.41250

Fig.5.52 Non-equality position of planet gear

Gear dimension output					
Standard	Thickness	Pair meshing	Others		
Description	symbol	unit	SUN GEAR	PLANET GEAR	RING GEAR
Transverse pressure angle	at	deg		20.00000	
Base helix angle	Betab	deg		0.00000	
Transverse circular pitch	Pbt	mm		5.3138	
Normal circular pitch	Pbn	mm		5.3138	
Lead	Lead	mm	0.0000	0.0000	0.0000
Base diameter	db	mm	25.3717	35.5204	94.7210
Reference pitch diameter	d	mm	27.0000	37.8000	100.8000
Minimum validity diameter (TF)	dt	mm	25.3861	35.7367	101.2005
Maximum validity diameter	dh	mm	31.3461	41.9329	108.8800
Addendum	ha	mm	2.1730	2.0664	-0.2003
Dedendum	hf	mm	1.8770	1.9836	4.2503
Whole depth	h	mm	4.0500	4.0500	4.0500
Addendum modification	xm	mm	0.3730	0.2664	2.0003
Normal profile shifted coefficient	xnc	---	0.1691	0.1066	1.1657

Fig.5.53 Result (Gear dimension)

Gear dimension output					
Standard	Thickness	Pair meshing	Others		
Description	symbol	unit	SUN GEAR	PLANET GEAR	RING GEAR
Operating transverse pressure	awt	deg	22.6897		26.2362
Operating helix angle	betaw	deg	0.0000		0.0000
Operating pitch diameter	dw	mm	27.5000	38.5000	39.6000
Operating Facewidth	bw	mm	20.0000		20.0000
Clearance	ck	mm	0.4105	0.4105	0.6838
Contact length	ga	mm	7.6176		7.9166
Near transverse contact ratio	Ka1	---	0.6996		1.0400
Far transverse contact ratio	Ka2	---	0.7339		0.4498
Transverse contact ratio	Ka	---	1.4335		1.4898
Overlap ratio	Kb	---	0.0000		0.0000
Total contact ratio	Kc	---	1.4335		1.4898
Sliding ratio at tip	Slipa	---	0.7264	0.8007	0.1341
Sliding ratio at root	Slipf	---	-4.0172	-2.6550	-1.0706
Transverse backlash	jnt	mm	0.0980		0.1180
Backlash angle	jSta	deg	0.4426	0.3162	0.3807
Total backlash angle(input axis)	jSta'	deg			0.9756 (Sun)
Maximum contact diameter	dja	mm	31.3461	41.9329	41.9329
Minimum contact diameter	djf	mm	25.5693	36.2134	36.1018

Fig.5.54 Result (Pair meshing)

Gear dimension output			
Standard	Thickness	Pair meshing	Others
Rotate ratio			
SUN	PLANET	RING	CARRIER
1.0000	-0.3521	0.0000	0.2113
Efficiency 0.9819			
RING GEAR interference			
Description	RING		
Involute	It doesn't		
Trochoid	It doesn't		
Triming	It doesn't		
Clearance(mm)			
Sun tip and Planet root	0.4105 (mm)		
Planet tip and Sun root	0.4105 (mm)		
Planet tip and Ring root	0.6838 (mm)		
Ring tip and Planet root	0.6838 (mm)		
Non-equality			

Fig. 5.55 Result (Efficiency, etc.)

By clicking "Uneven layout setting" on the toolbar, Fig. 5.56 is displayed. As for the indication of unequal arrangement, the [A1] gear in Figure 5.56 is the reference gear. Also, since the unequal arrangement angle can not be input arbitrarily, select from the angle table shown in [B] of Fig. 5.57. There are 71 types of arrangement angles of planetary gears in the example.

The arrangement is shown in Fig. 5.58 so that the tip circle of the [A2] gear and [A3] gear does not come in contact with clicking the "minimum arrangement" in Fig. 5.56.

Now, the tooth shape meshing in the case of selecting the second 10.1408 ° from the angle of "B" in Fig. 5.57 is shown in Fig. 5.59. An enlarged view of [C] is shown in Fig. 5.60, and tooth rendering is shown in Fig. 5.61.

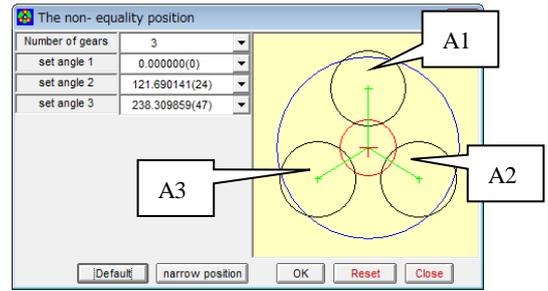


Fig.5.56 Non-equality position-1

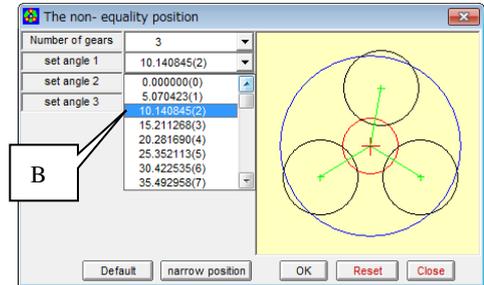


Fig.5.57 Non-equality position-2

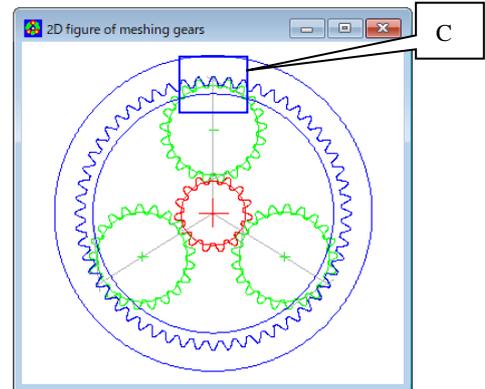


Fig.5.58 Non-equality position of planet gear

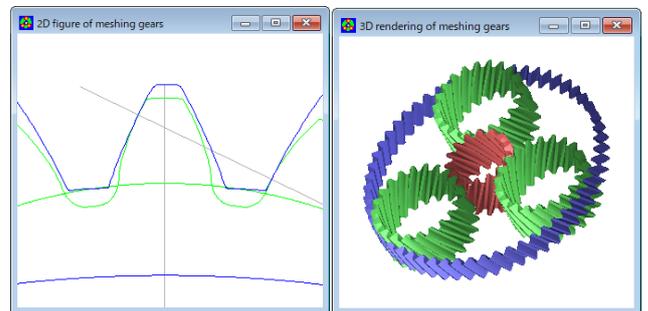


Fig5.59 [C] in Fig.5.58

Fig.5.60 Tooth rendering

In addition, strength calculation, tooth profile data file output, etc. are the same as the basic software. Calculation examples when the number of planets is 5 are shown in Figure 5.62 to 5.64.

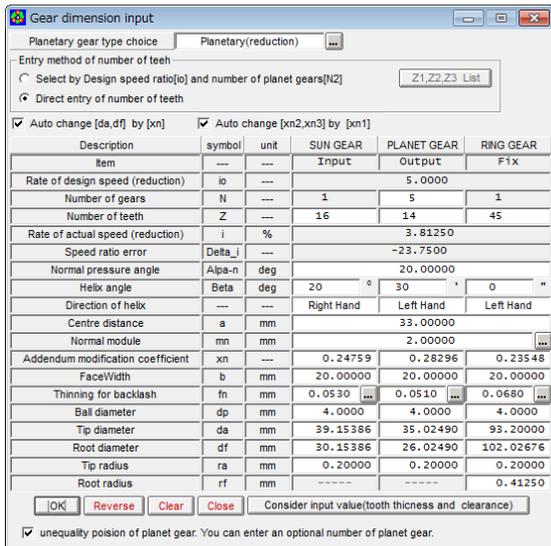


Fig.5.62 Non-equality position of planet gear design

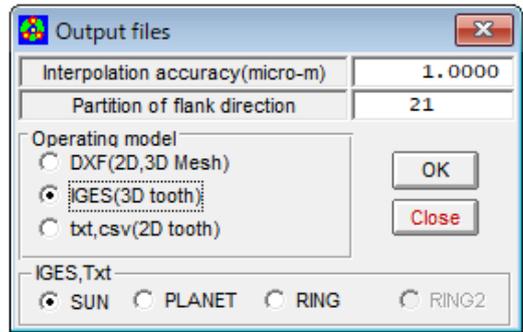


Fig. 5.65 Output file setting

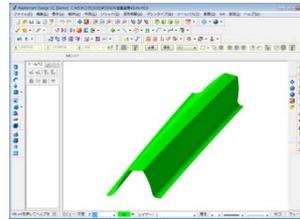


Fig. 5.66 CAD (sun gear)

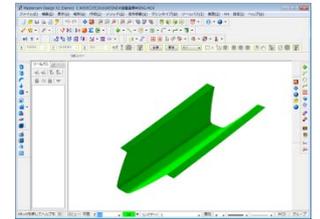


Fig. 5.67 CAD (ring gear)

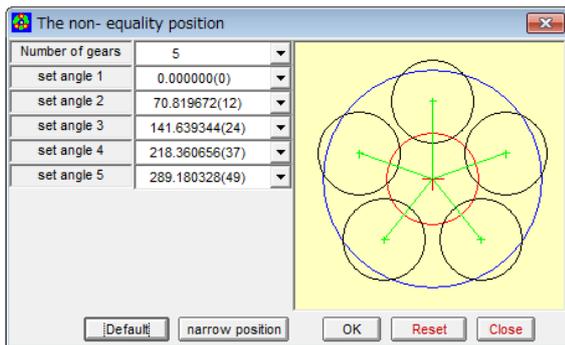


Fig.5.63 Non-equality position-3

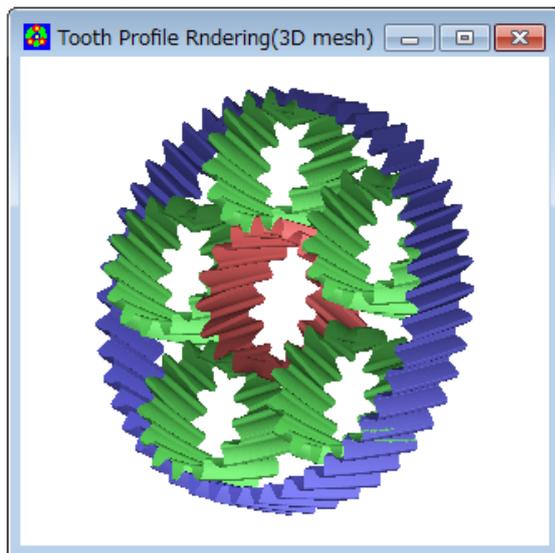


Fig.5.64 Tooth rendering

### 5.15 Tooth profile data file output

The tooth profile of the generated gear can be output as a file in Figure 5.65. Fig. 5.66 and Fig. 5.67 show CAD drawing examples.